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NATIONAL OCEANIC AND ATMOSPHERIC ADMINISTRATION
NATIONAL WEATHER SERVICE
NATIONAL METEOROLOGICAL CENTER

OFFICE NOTE 377

Skill of Medium Range Forecasts

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This is an unreviewed manuscript, primarily intended for informal exchange of information among NMC staff members.

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PURPOSE

This paper depicts in a graphical manner the skill of the Medium Range (3-10 day) man and machine (numerical model guidance) forecasts. It will be updated each February in order to present the latest scores for each of the several forecast categories in the medium range forecast program (MRFP). Only scores with at least a 5-year period of record are presented. This paper contains the standardized and unstandardized mean sea level pressure and 500mb correlation; the Gilman precipitation skill; the minimum/maximum average absolute temperature error; and the 5-day mean normalized 500mb correlation, temperature, and precipitation skill scores.

Figure 1 depicts the North American (NOAM, 130 grid points) and United States (US, 88 grid points) mean sea level pressure (MSLP) and 500mb correlation score verification areas.

Figure 2 is a plot of the calendar year 1990 seasonal and 10 year (1980-1989) average seasonal (darker lines) standardized correlation scores for the man (official) NOAM area MSLP progs verifying on days 3, 4, and 5 after forecast day. (See appendix A for an explanation of this score).

Figure 3 is similar to Figure 2 except scores are for the NMC/NWP model progs.

Figure 4 is a plot of the 23/21 year (1968/70-1990) standardized correlation scores for the man (official) and NMC/NWP model NOAM area MSLP progs verifying on days 3, 4, and 5 after forecast day.

Figure 5 is a plot of the 13 year (1978-1990) average seasonal unstandardized correlation scores for the man (official), NMC/NWP model (darker lines), and climatology US area MSLP progs verifying on days 3, 4, and 5 after forecast day.

Figure 6 is similar to Figure 3 except the level is 500mb.

Figure 7 is similar to Figure 4 except the level is 500mb.

Figure 8 is a plot of the calendar year 1990 monthly standardized correlation scores for the man (official), MRF model, and ECMWF model NOAM area 500 mb mean progs verifying on days 6-10 after forecast day.

Figure 9 is similar to Figure 8 except scores are for a 7 year average (1984-1990).

Figure 10 is a plot of the 11 year (1980-1990) standardized correlation scores for the man (official), NMC/NWP model, and ECMWF model (82-90) NOAM area 500mb progs verifying on days 6-10 after forecast day.

Figure 11 depicts the 41/61 stations in the US where the 1-5/6-10 day temperature forecasts are verified.

Figure 12 is a plot of the calendar year 1990 bi-monthly and 10 year (1980-1989) average bi-monthly (darker lines) US area temperature forecasts verifying on days 3, 4, and 5 after forecast day.

Figure 13 is similar to Figure 12 except scores are for the maximum.

Figure 14 is a plot of the 20 year (1971-1990) absolute error minimum temperature scores for the man (official) and climatology US area temperature forecasts verifying on days 3, 4, and 5 after

and 5 after forecast day.

Figure 15 is similar to Figure 14 except scores are for the maximum.

Figure 16 is a plot of the 20 year (1971-1990) absolute error (minimum + maximum)/2 temperature scores for the man (official), perfect prog, and climatology US area temperature forecasts verifying on days (3+4+5)/3 after forecast day.

Figure 17 is a plot of the 13 year (1978-1990) 3-class and 5-class temperature skill scores for the man (official) and persistence US area categorical temperature forecasts verifying on days 6-10 after forecast day. (See appendix B for an explanation of this score).

Figure 18 depicts the 100 stations in the US where the precipitation forecasts are verified.

Figure 19 is an example of a day 3, 4, or 5 precipitation forecast. The dashed lines are the 24-hour departure from probability of precipitation (DN POP) forecast for January 3. The solid lines are the 24-hour climatological (normal) probability of precipitation (NPOP) for the first 15 days of January. A total of (DN POP + NPOP) > 30 is considered "yes" forecast of precipitation (> 0.01 inch). All stations with an (NPOP) > 30 are considered as a "yes" climatological forecast of precipitation.

Figure 20 is a plot of the calendar year 1990 seasonal and 10 year (1980-1989) average seasonal (darker lines) Gilman precipitation skill scores for the man (official) US area precipitation forecasts verifying on days 3, 4, and 5 after forecast day. (See appendix C for an explanation of this score).

Figure 21 is a plot of the 21 year (1970-1990) Gilman precipitation skill scores for the man (official) and climatology US area precipitation forecasts verifying on days 3, 4, and 5 after forecast day.

Figure 22 is a plot of the 13 year (1978-1990) 3-class precipitation skill scores for the man (official), NMC/NWP model, and climatology US area categorical precipitation forecasts verifying on days 1-5 after forecast day. (See appendix D for an explanation of this score).

Figure 23 is similar to Figure 22 except the forecasts are for days 6-10 after forecast day.

SECTION 1

Man and Machine (NMC/NWP Model Guidance)

Mean Sea Level Pressure and 500mb Correlation Scores

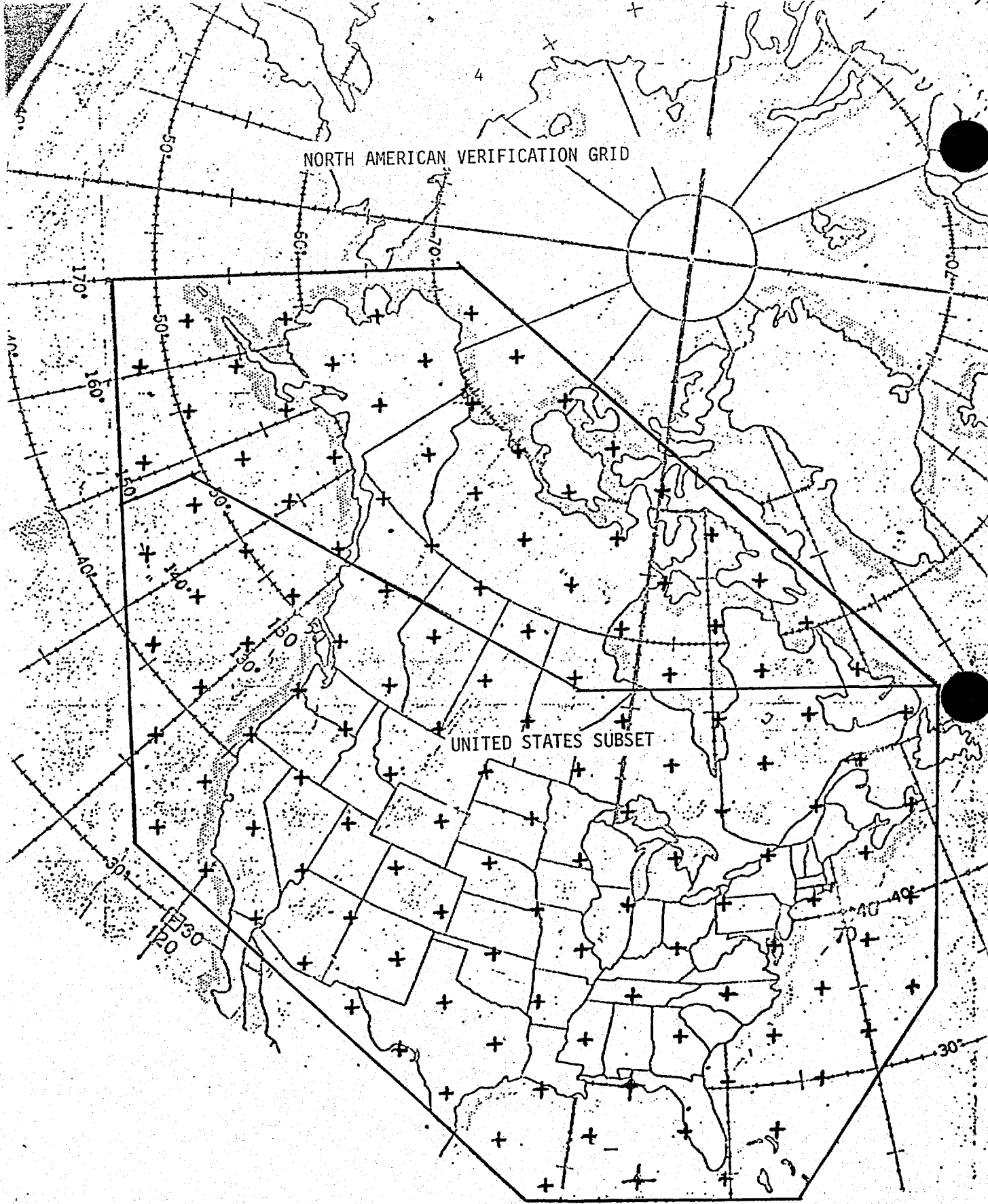


Figure 1

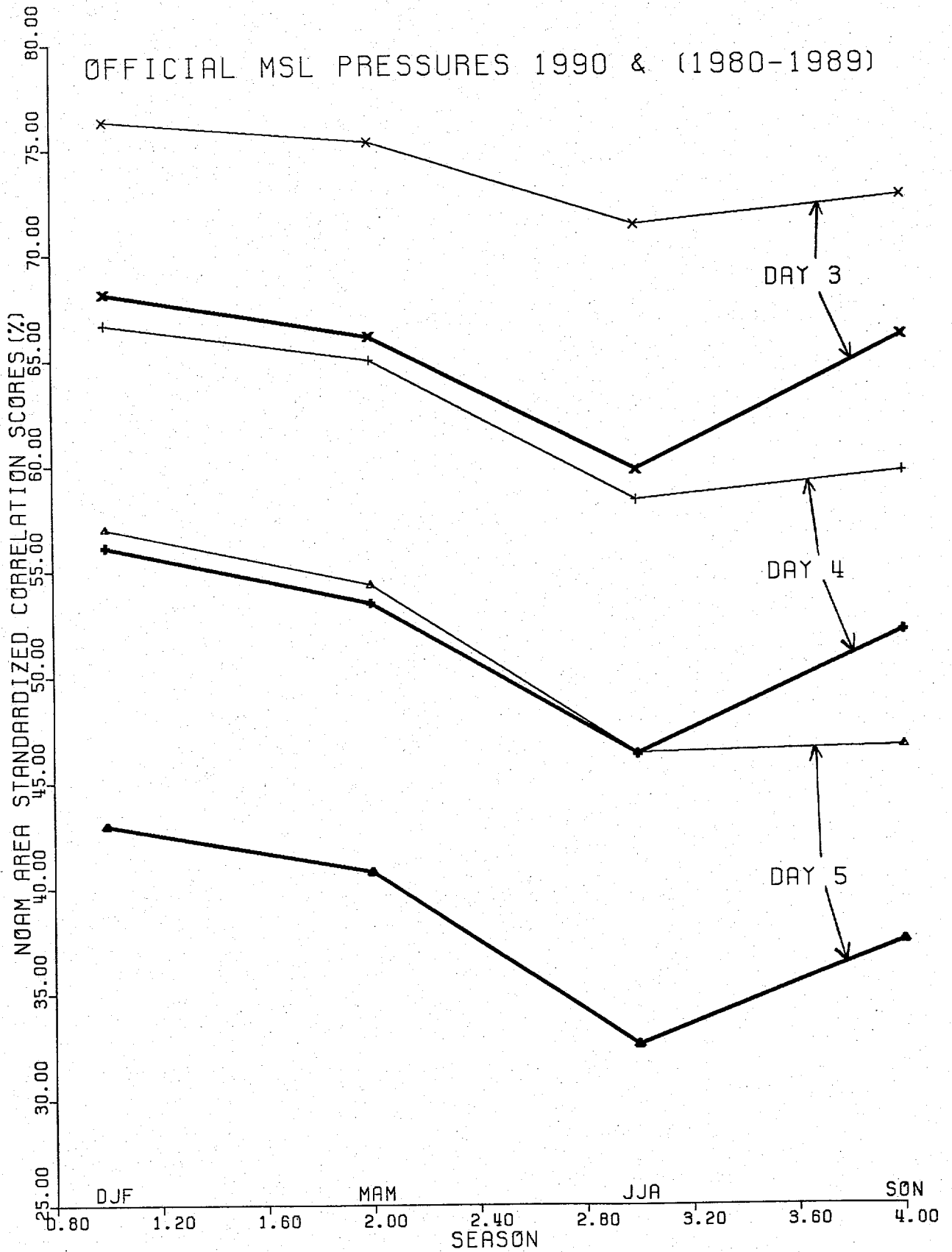


Figure 2

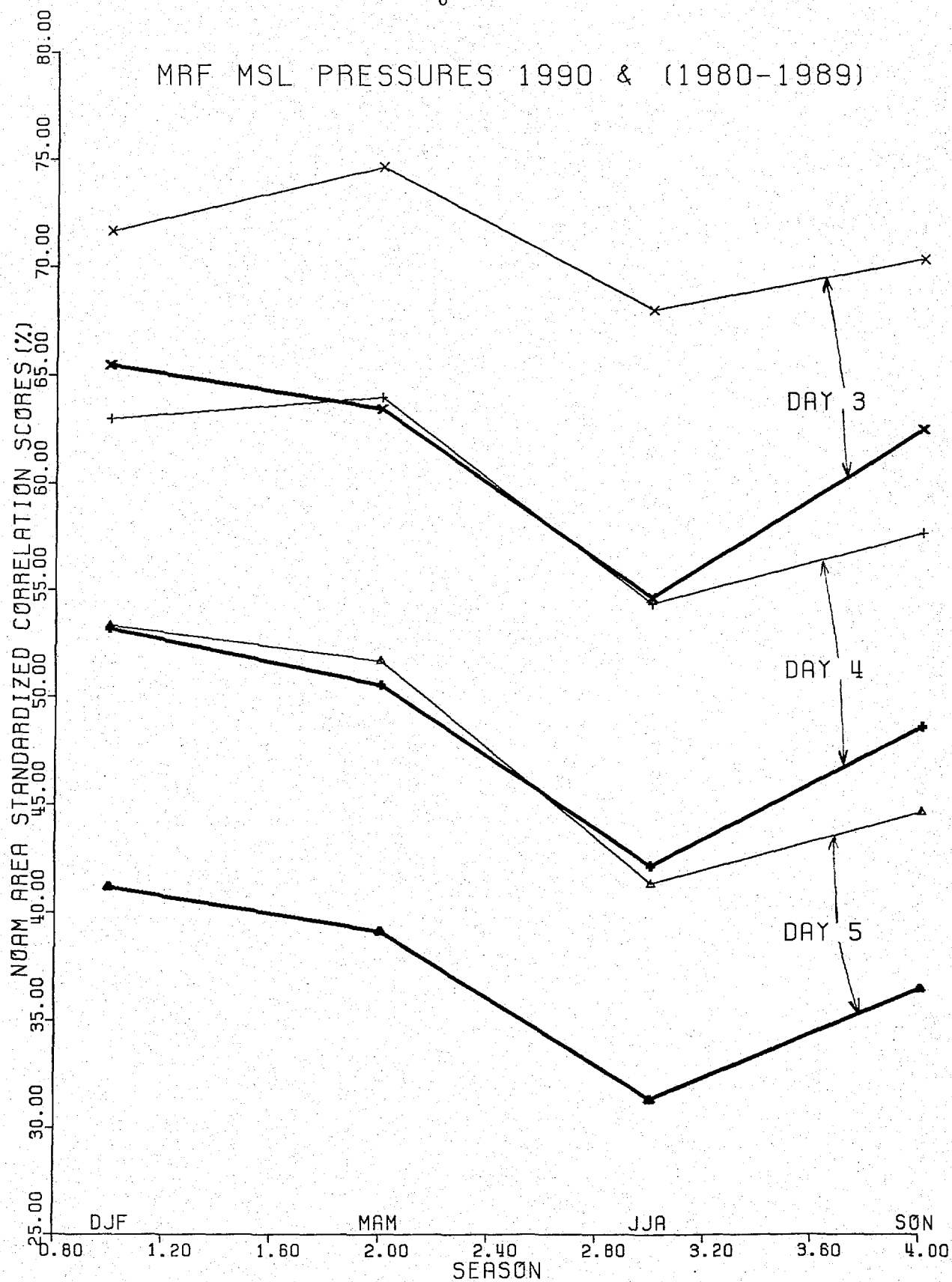


Figure 3

OFFICIAL & NWP MODEL MSL PRESSURES
1968-1990

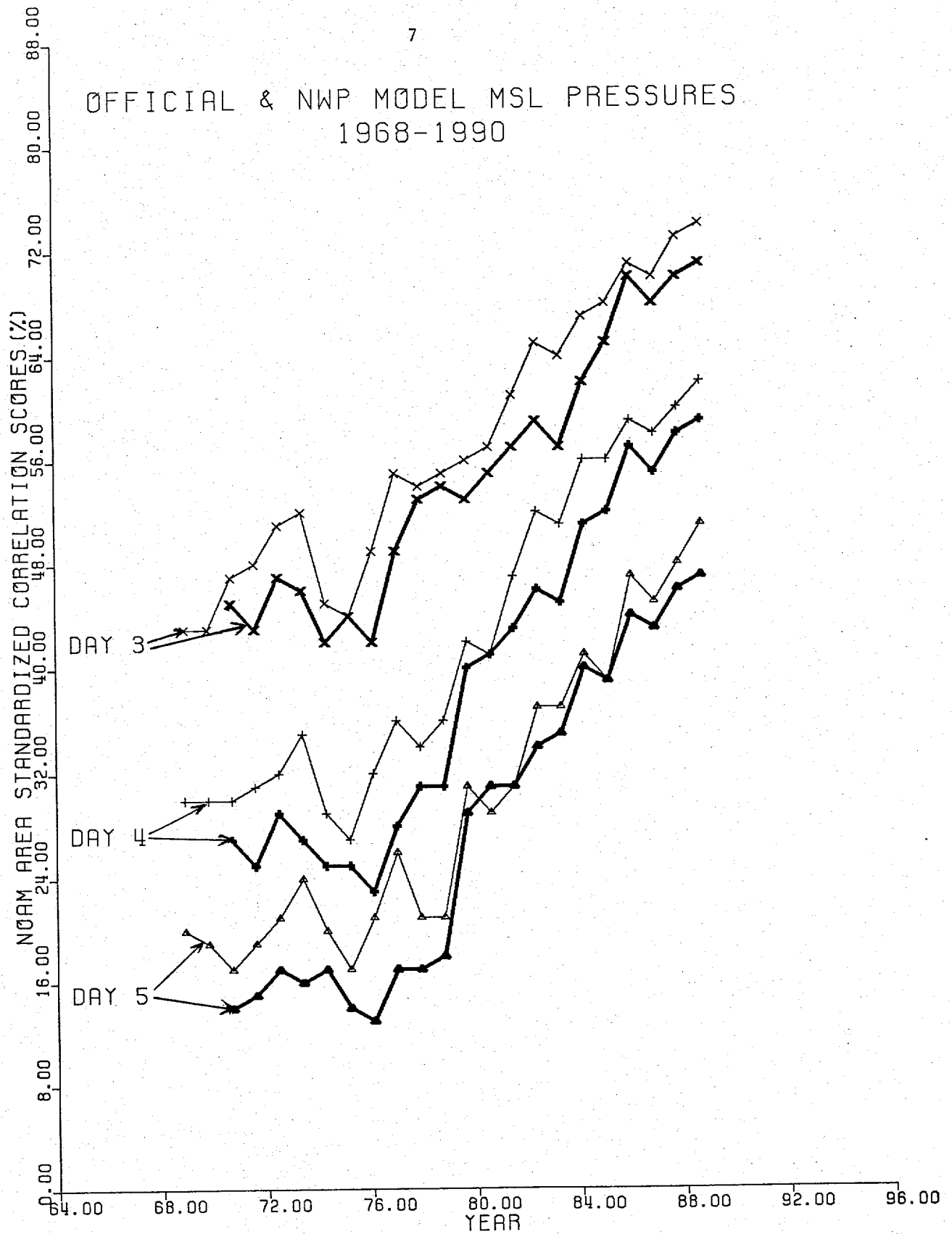


Figure 4

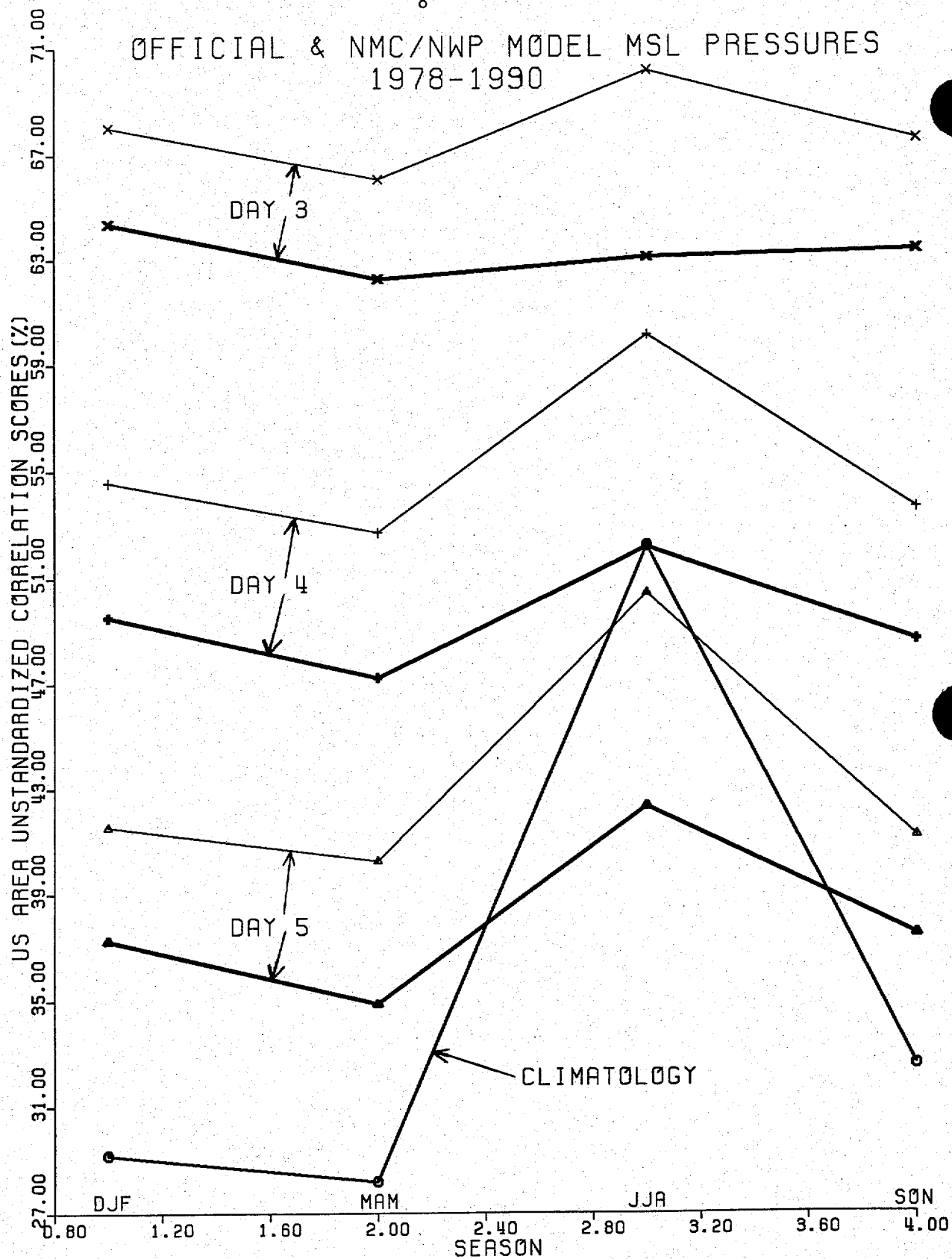


Figure 5

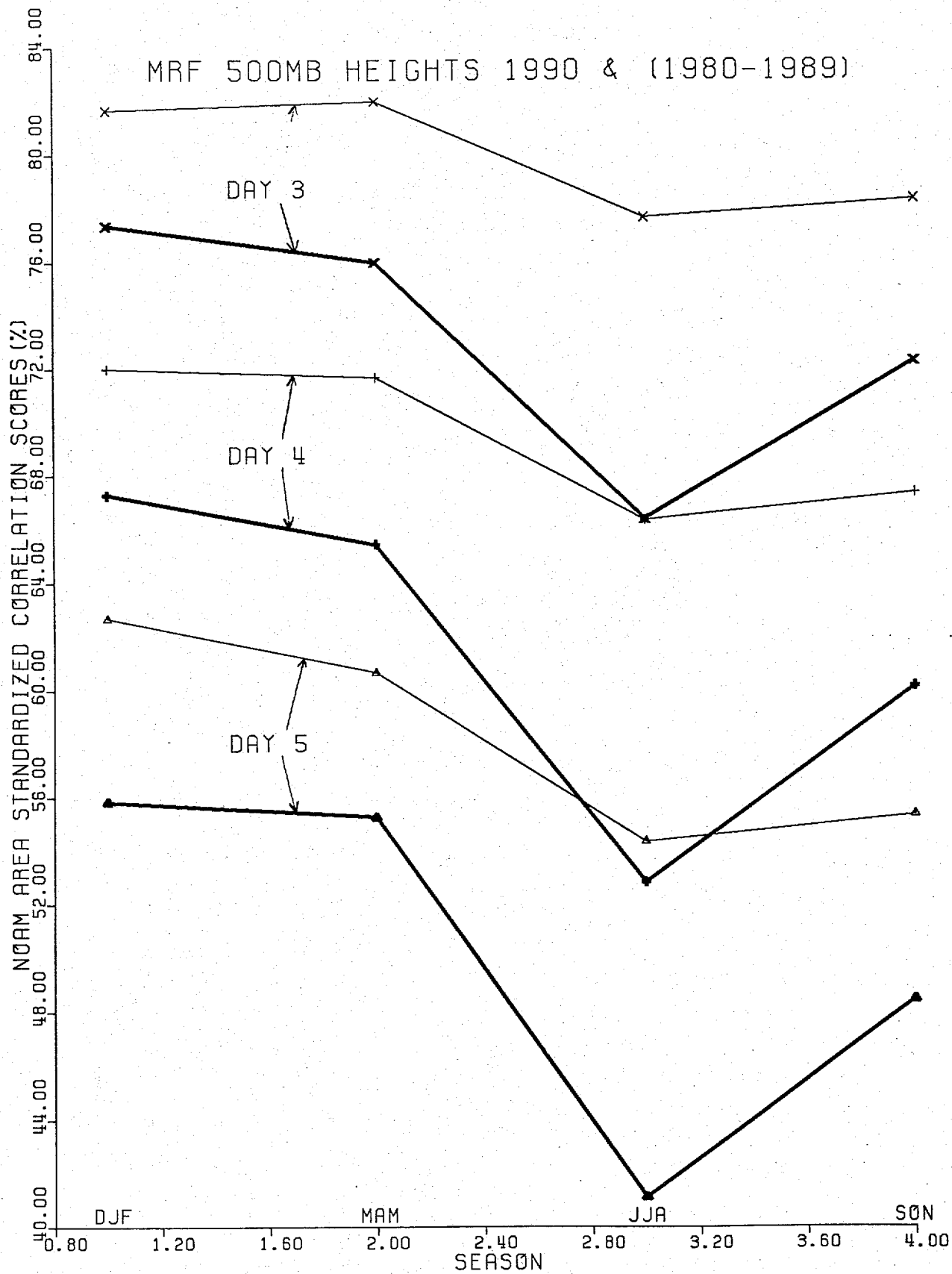


Figure 6

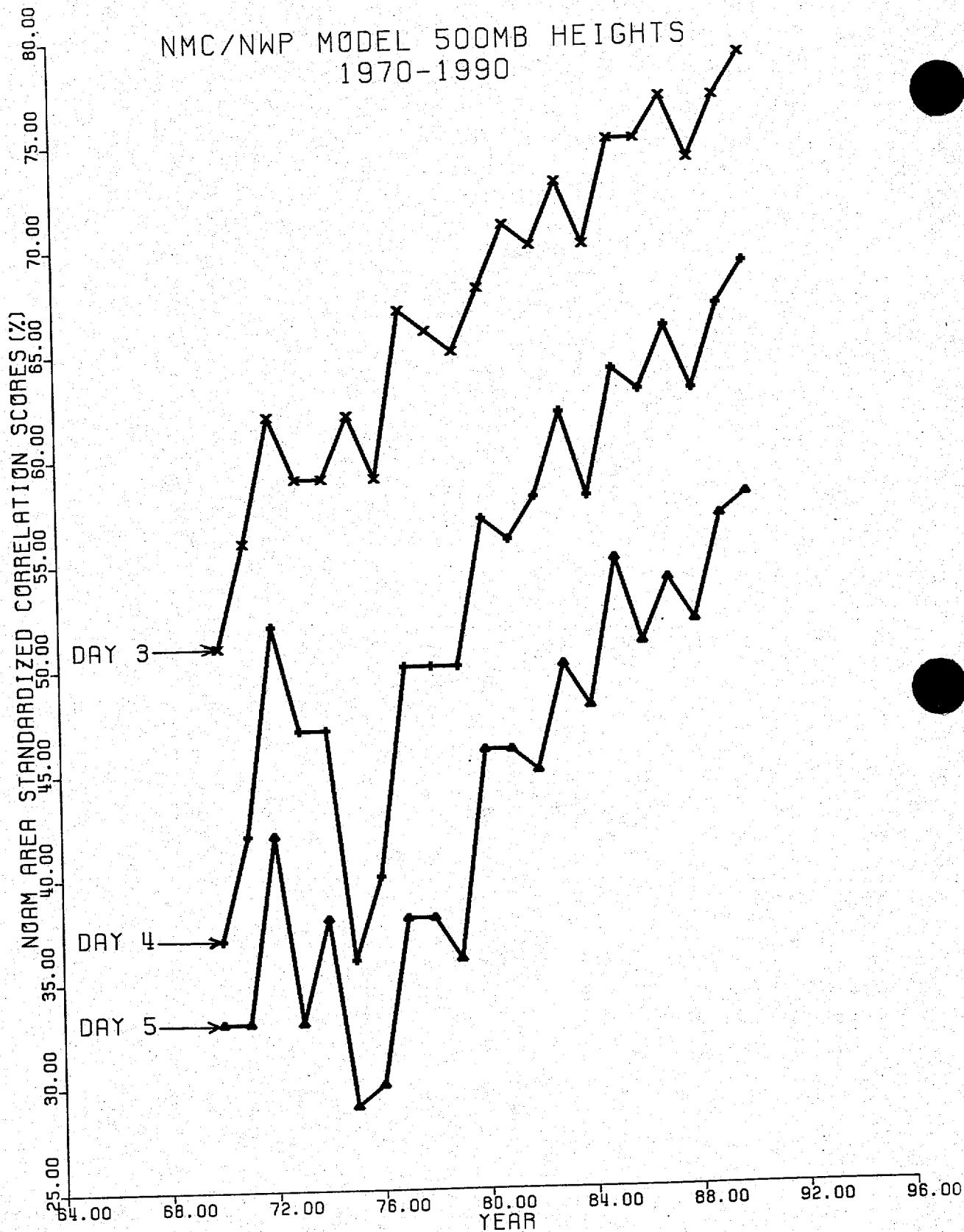


Figure 7

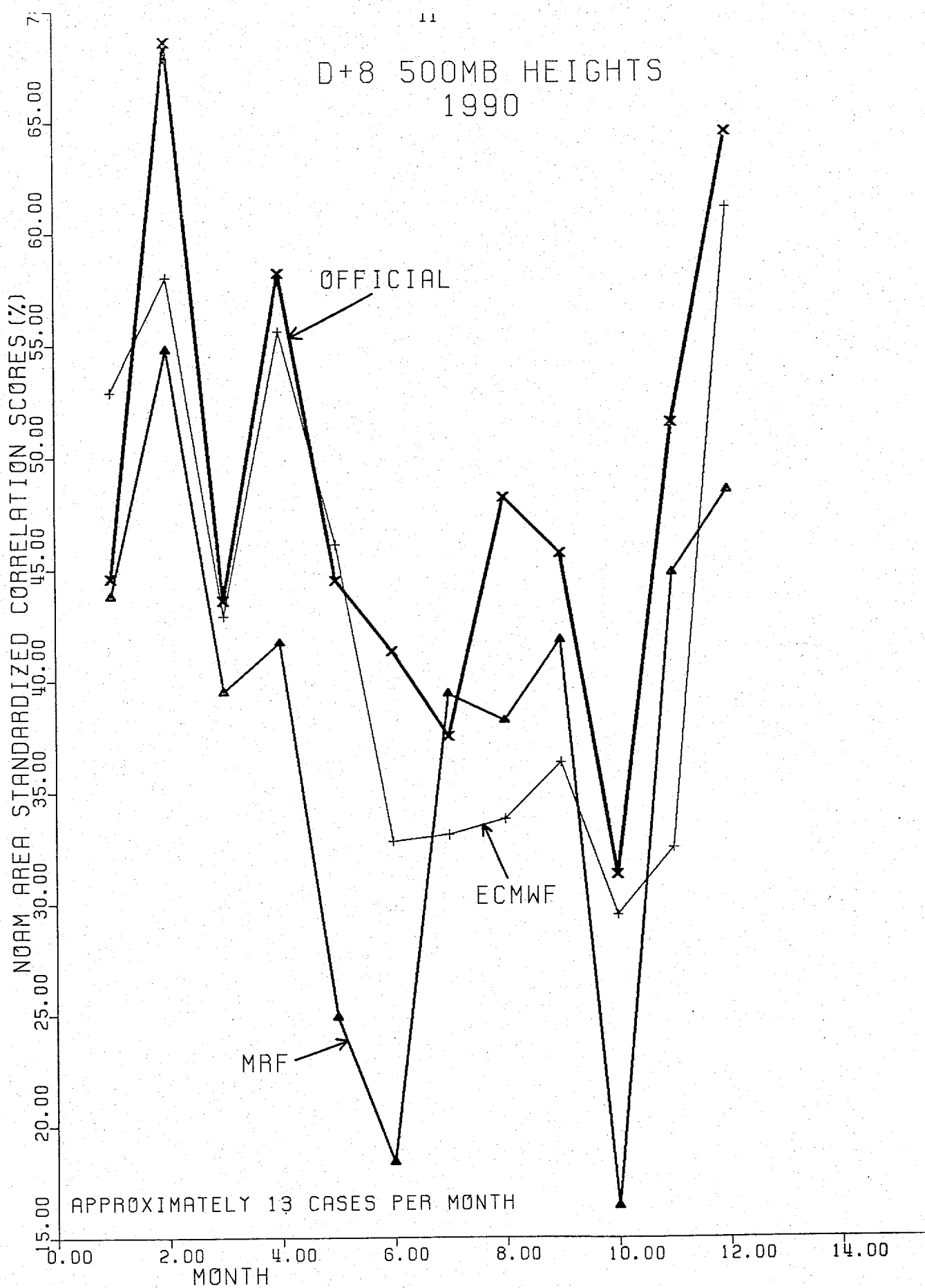


Figure 8

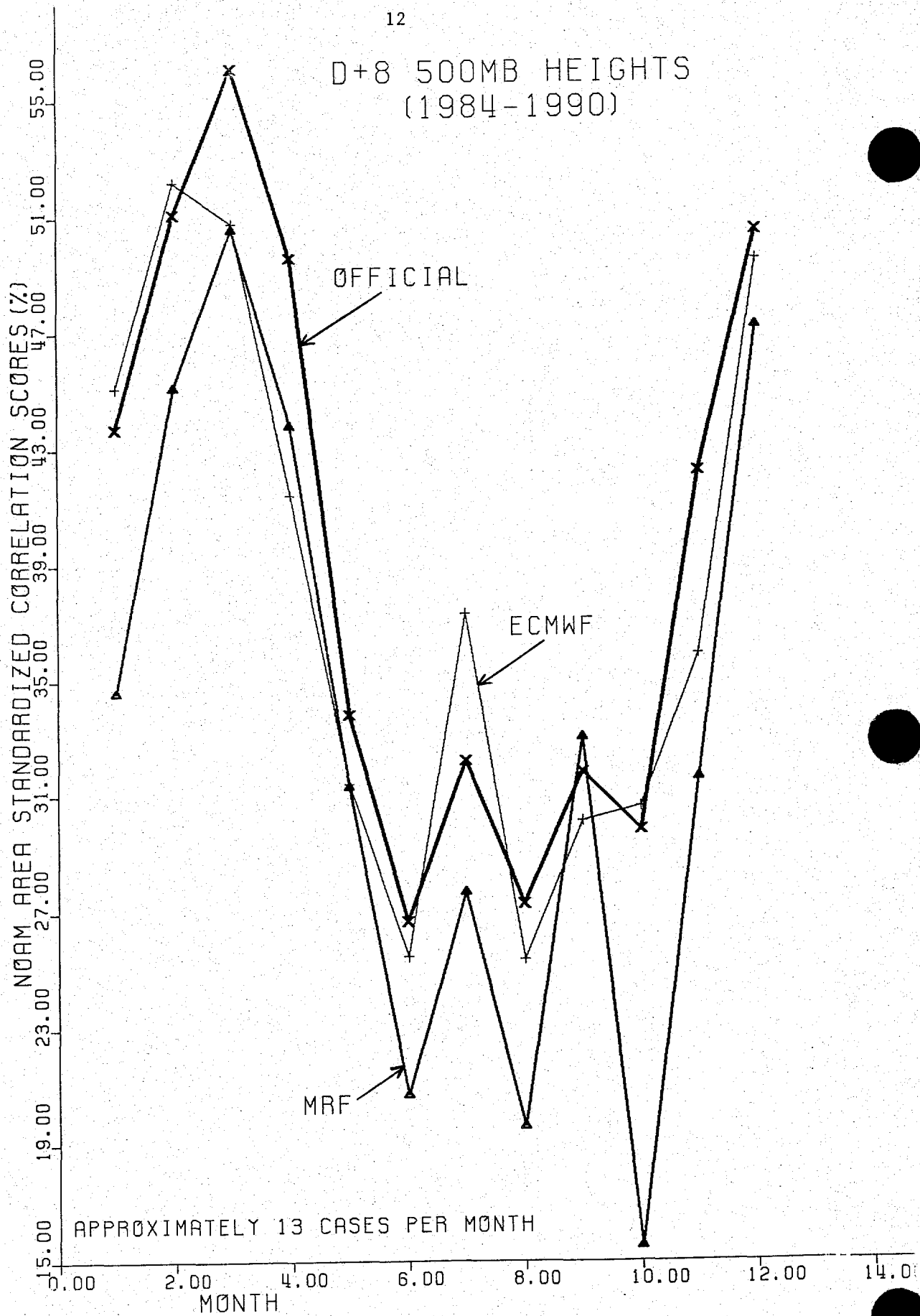
D+8 500MB HEIGHTS
(1984-1990)

Figure 9

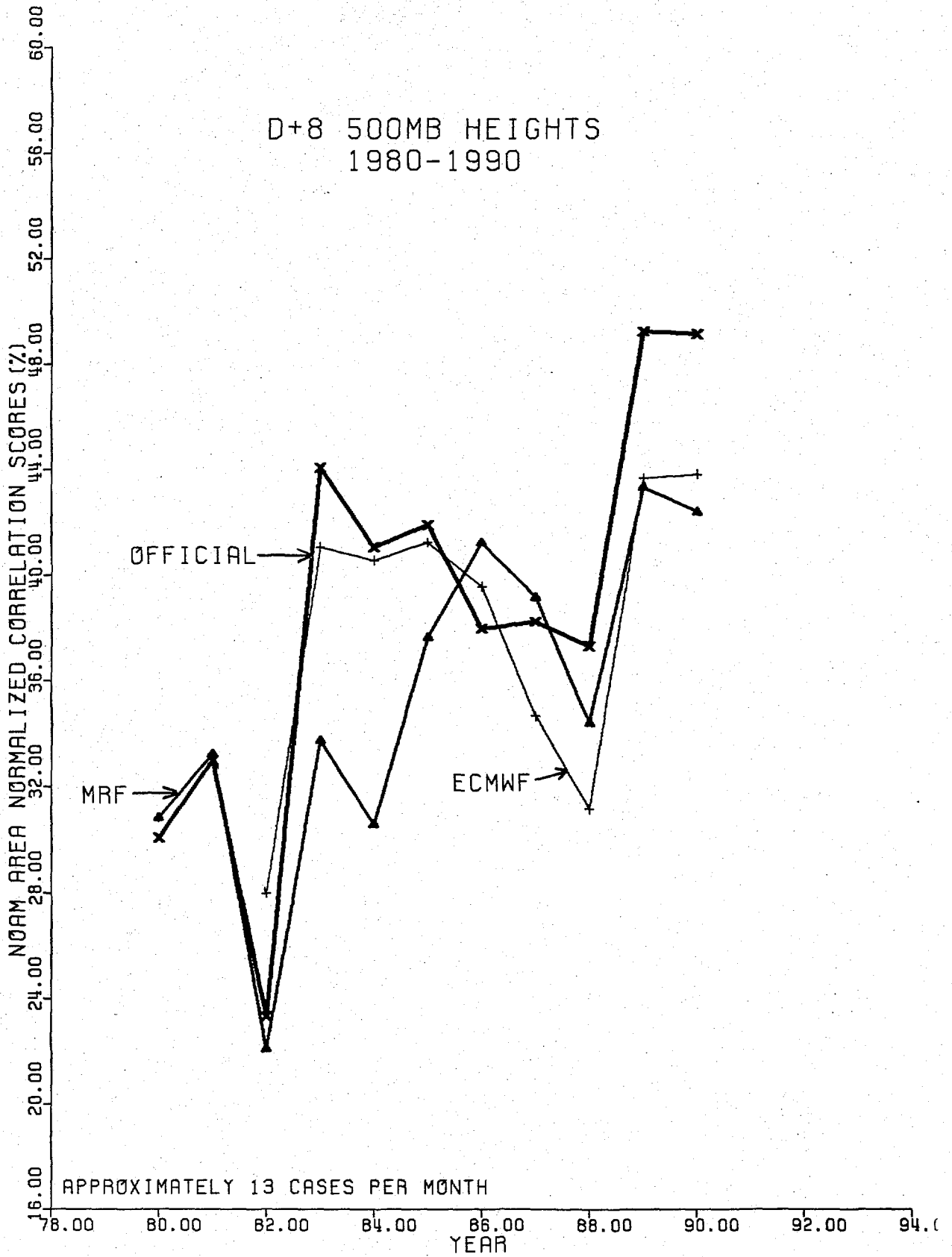
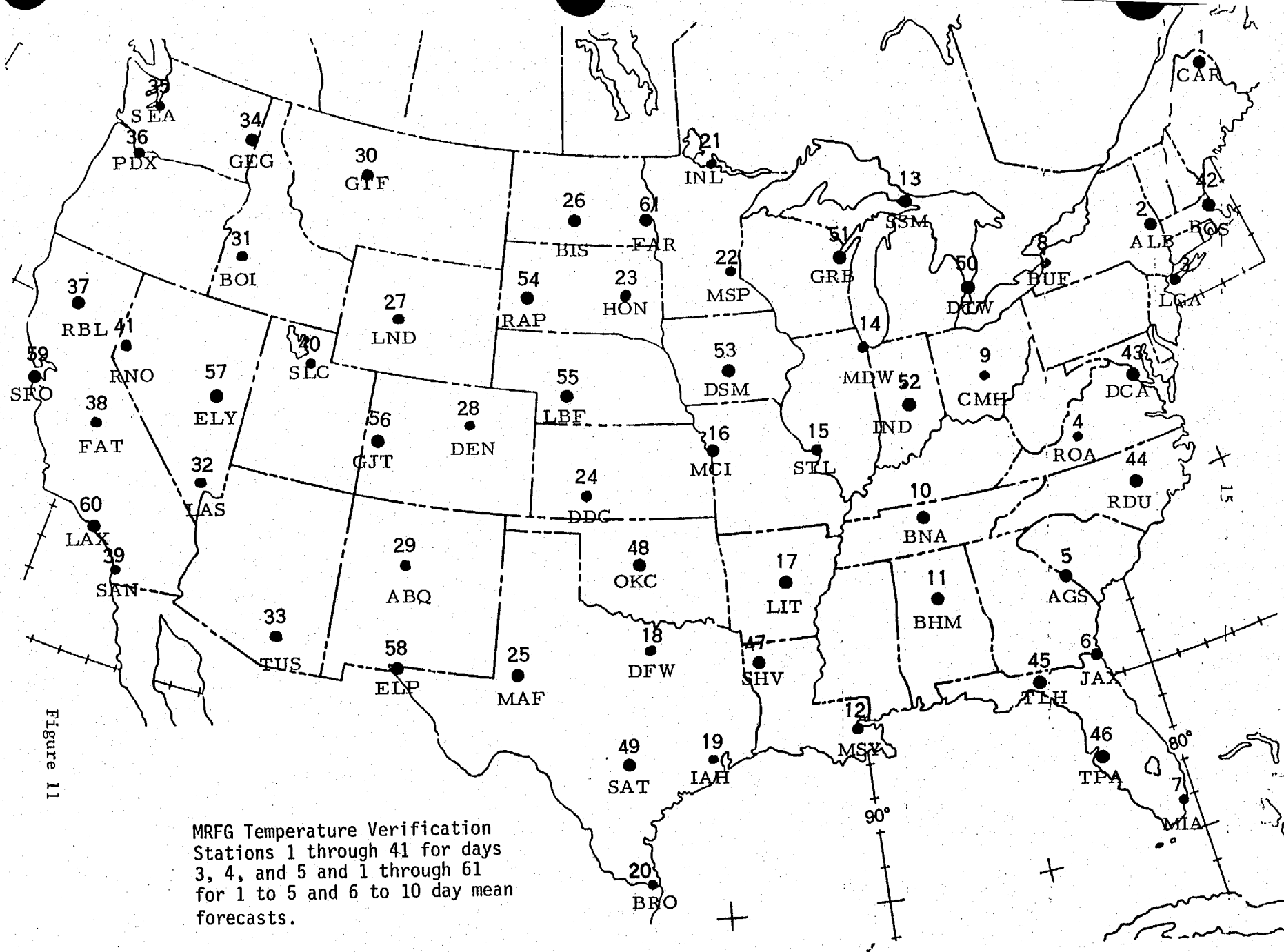


Figure 10

SECTION 2

Man and Machine (Klein-Lewis Perfect Prog Guidance) Average

Absolute Error Temperature Scores



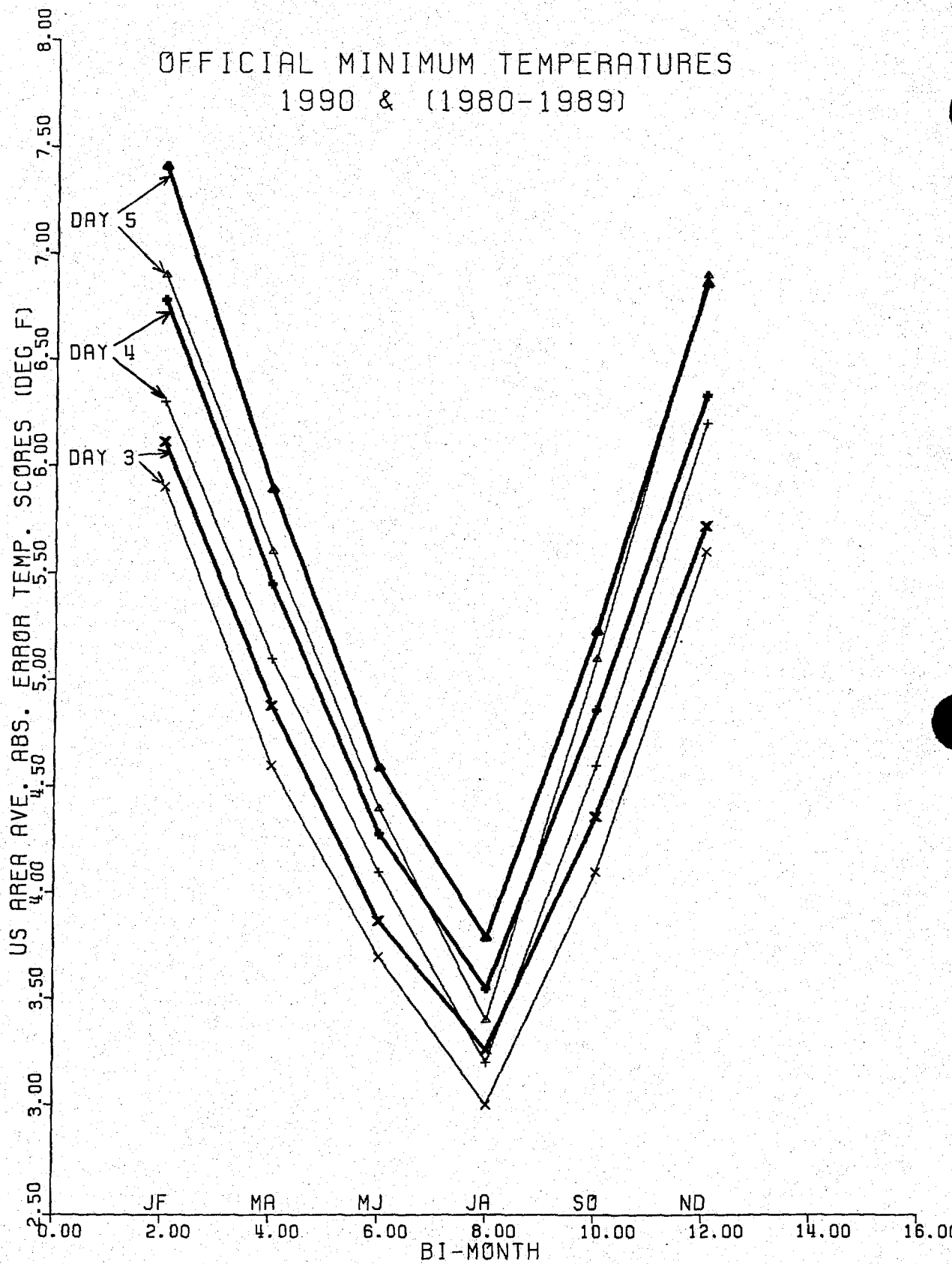


Figure 12

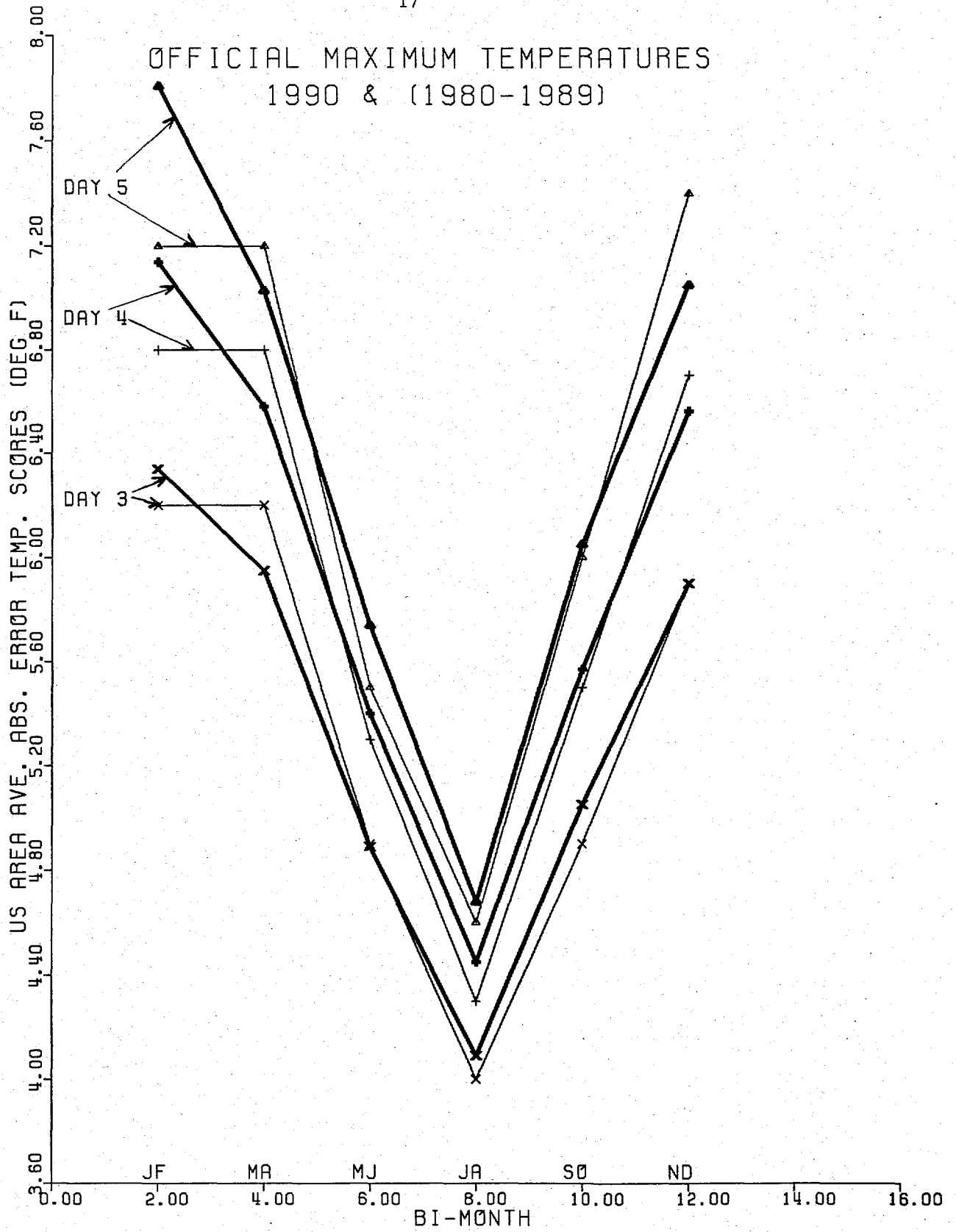


Figure 13

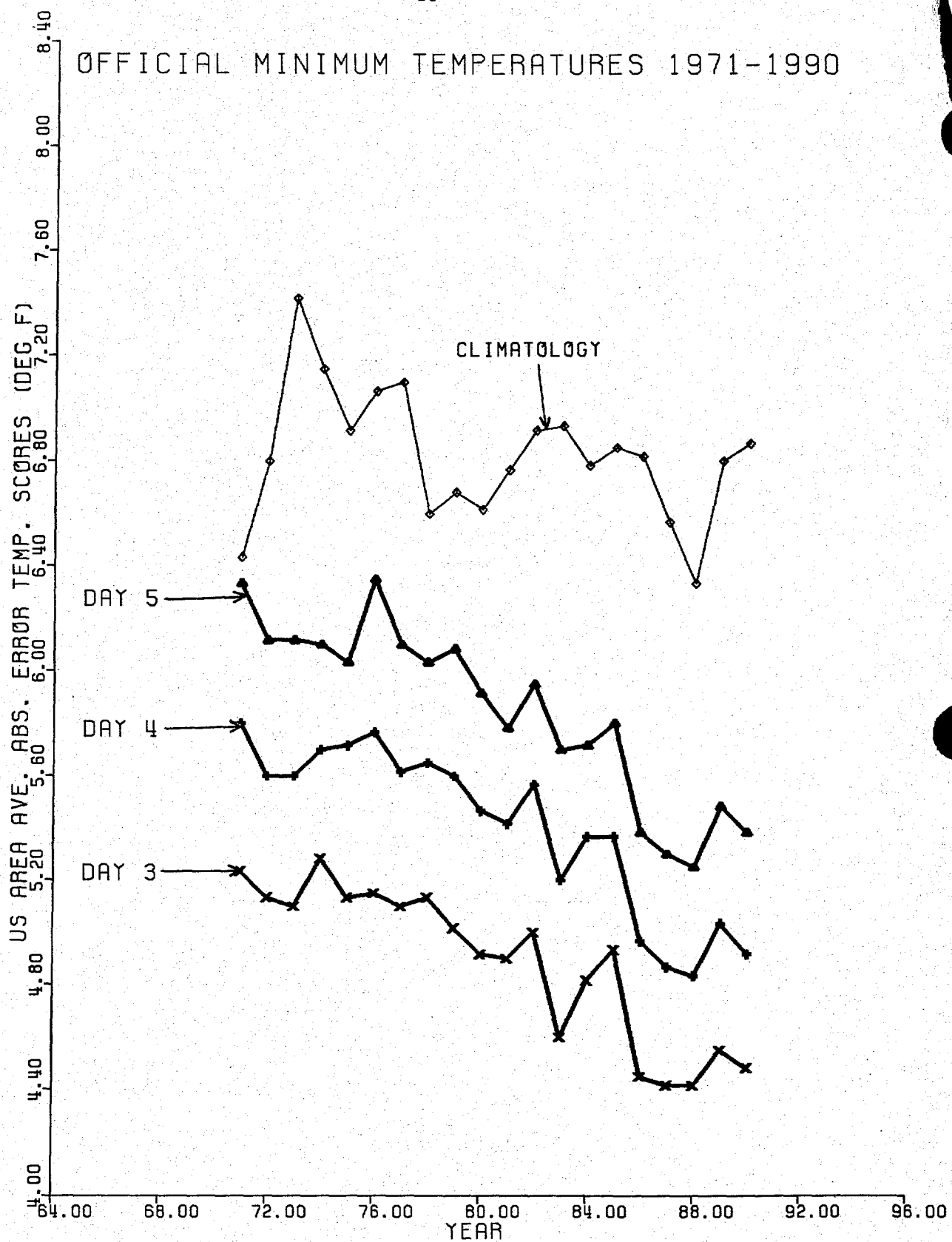


Figure 14

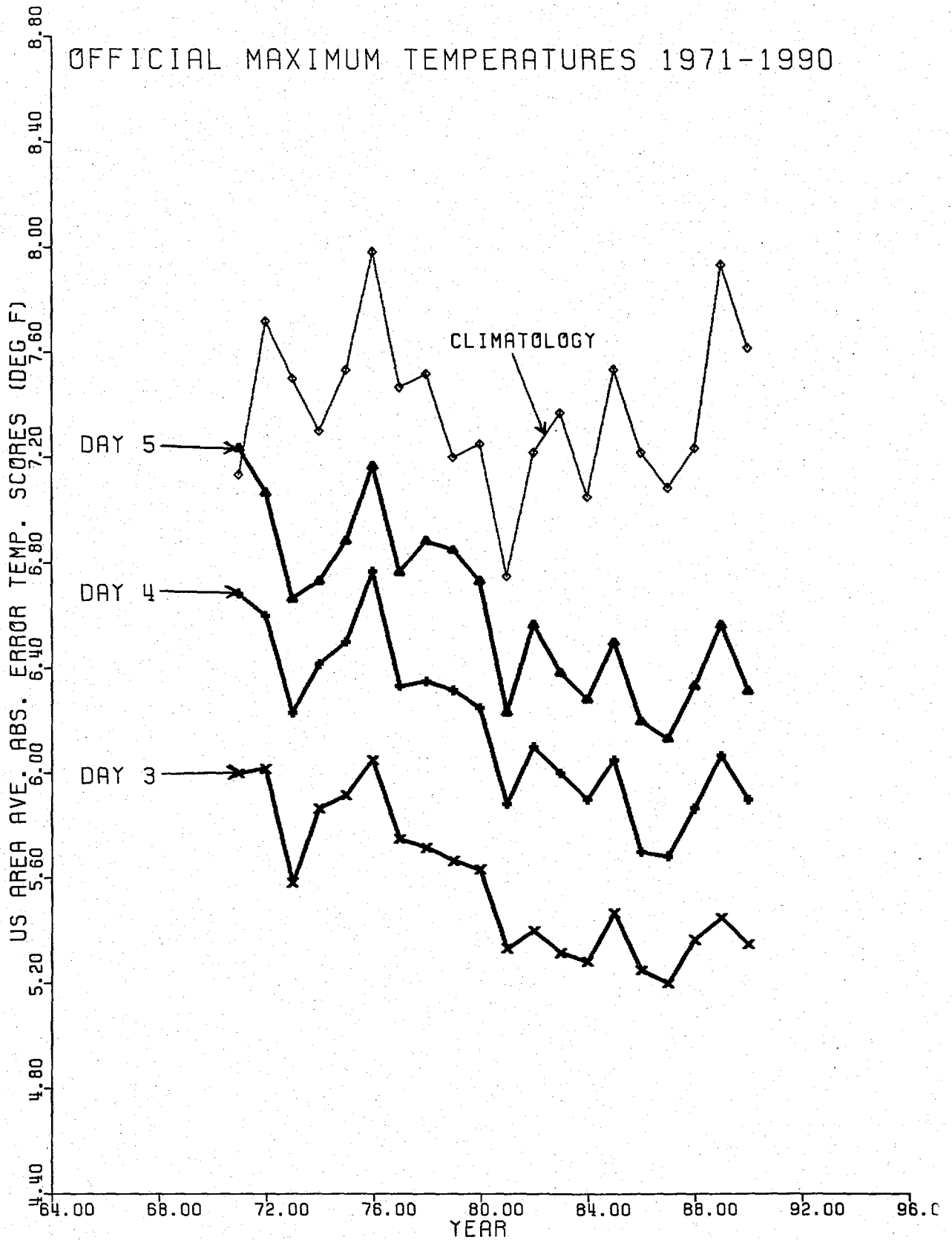


Figure 15

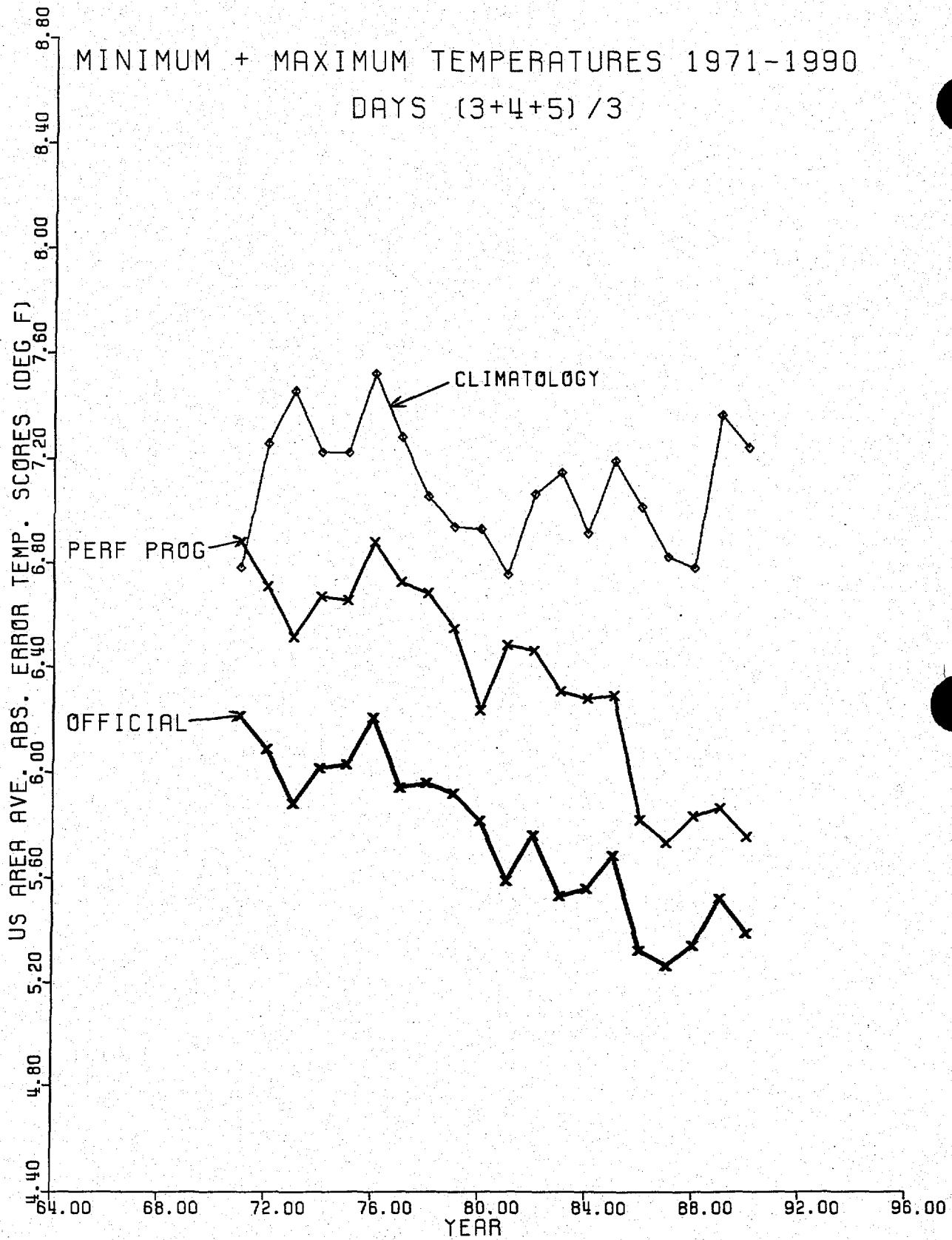


Figure 16

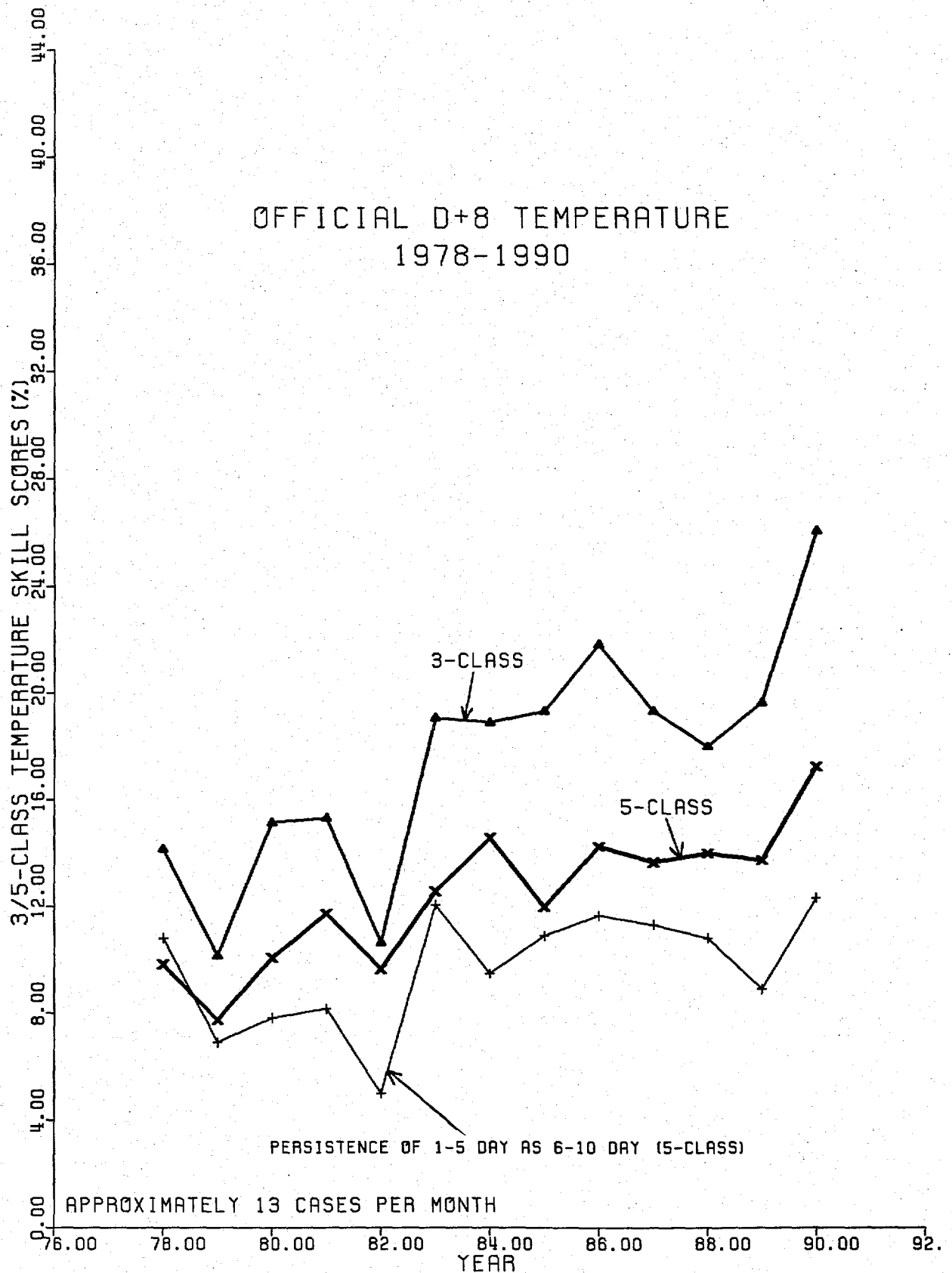
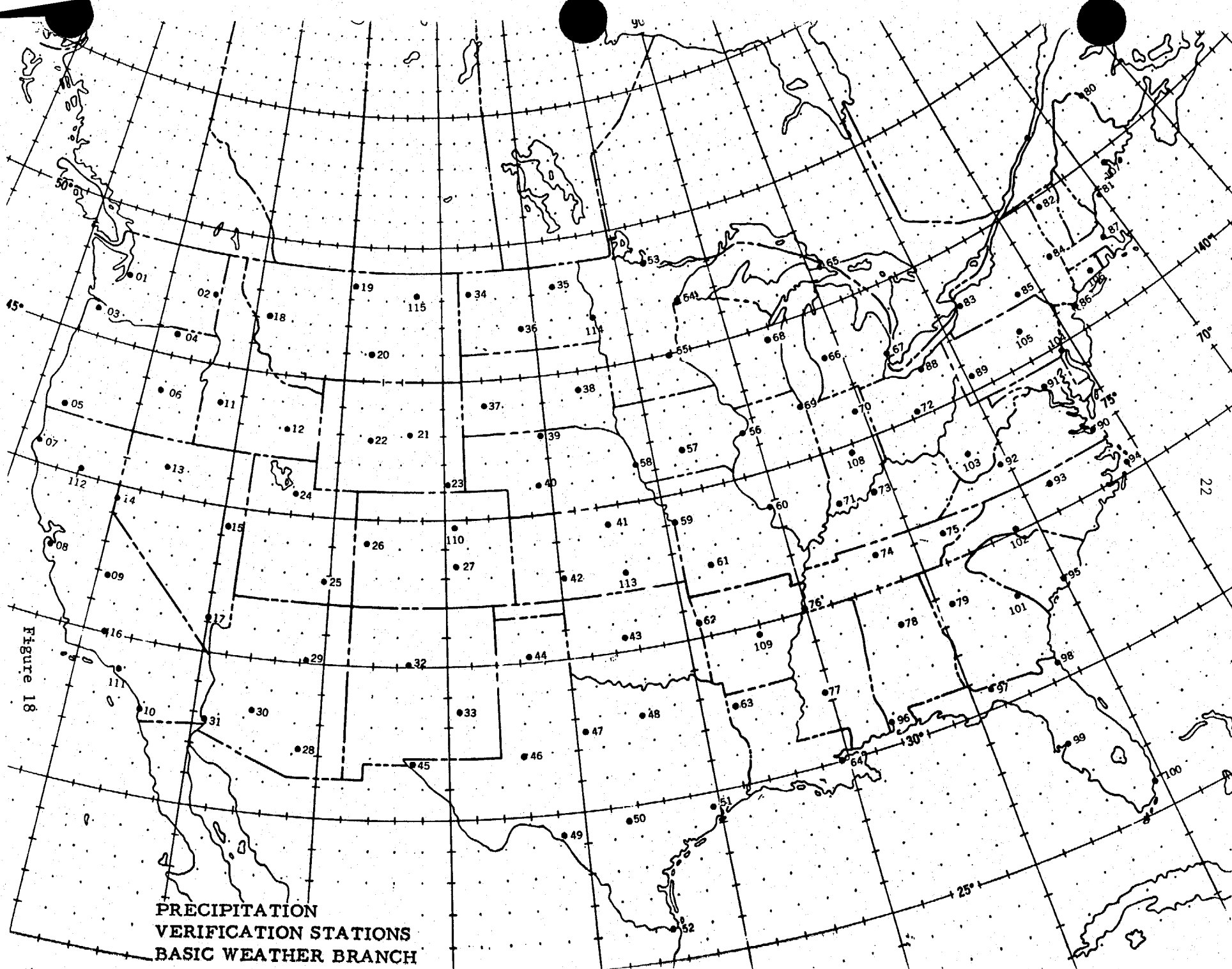


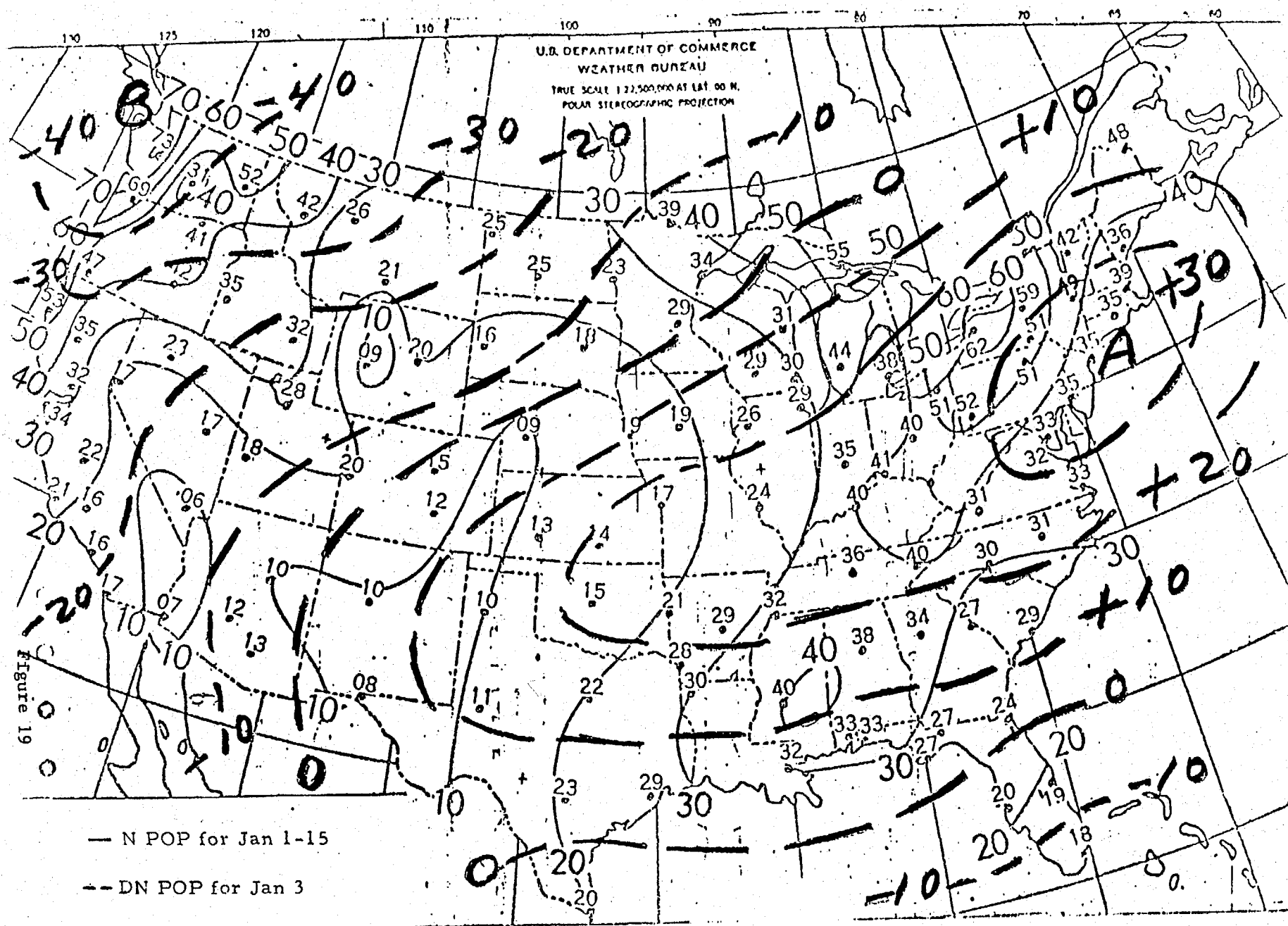
Figure 17

SECTION 3

Man and Machine (NMC/NWP Model Guidance)

Precipitation Skill Scores





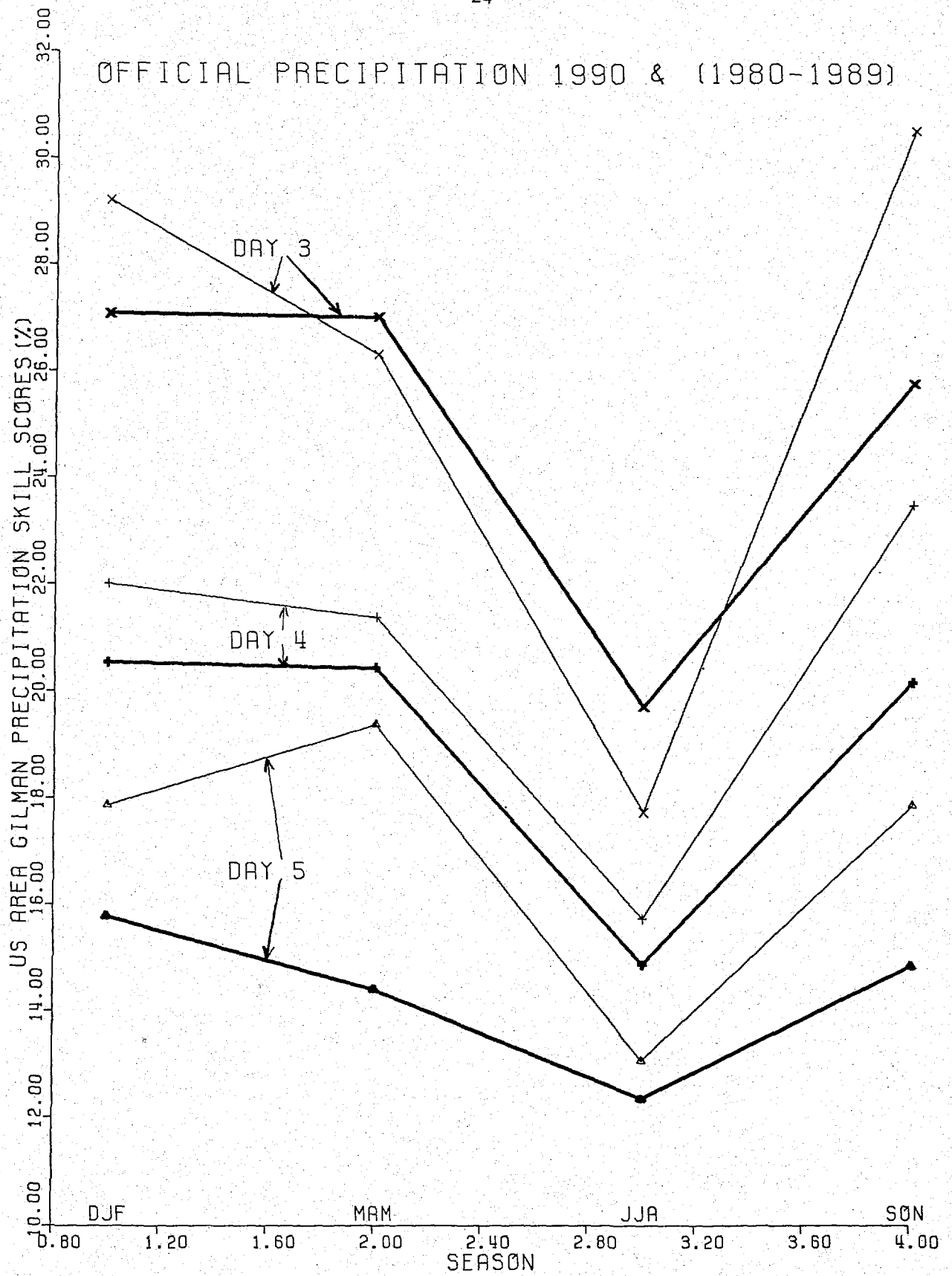


Figure 20

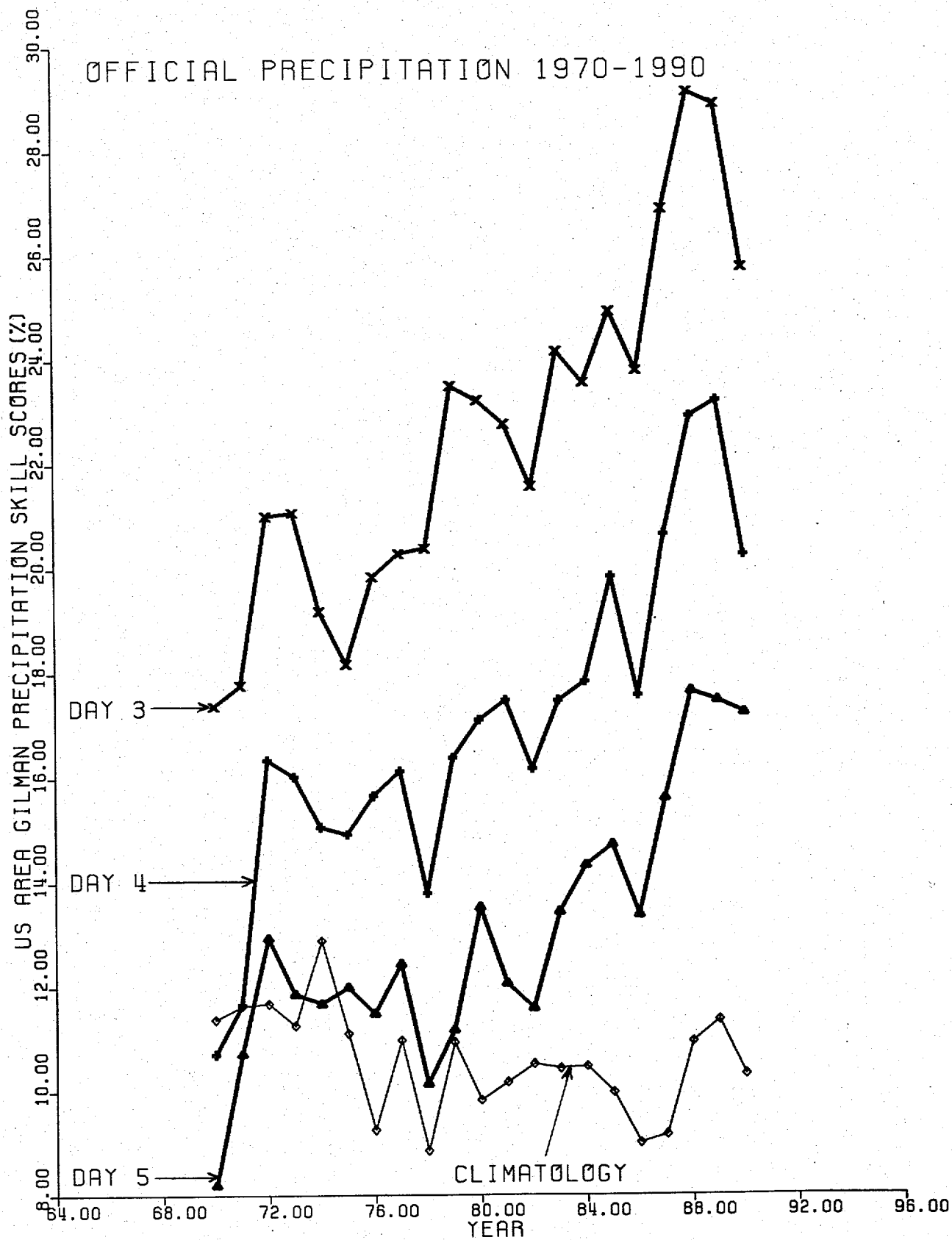


Figure 21

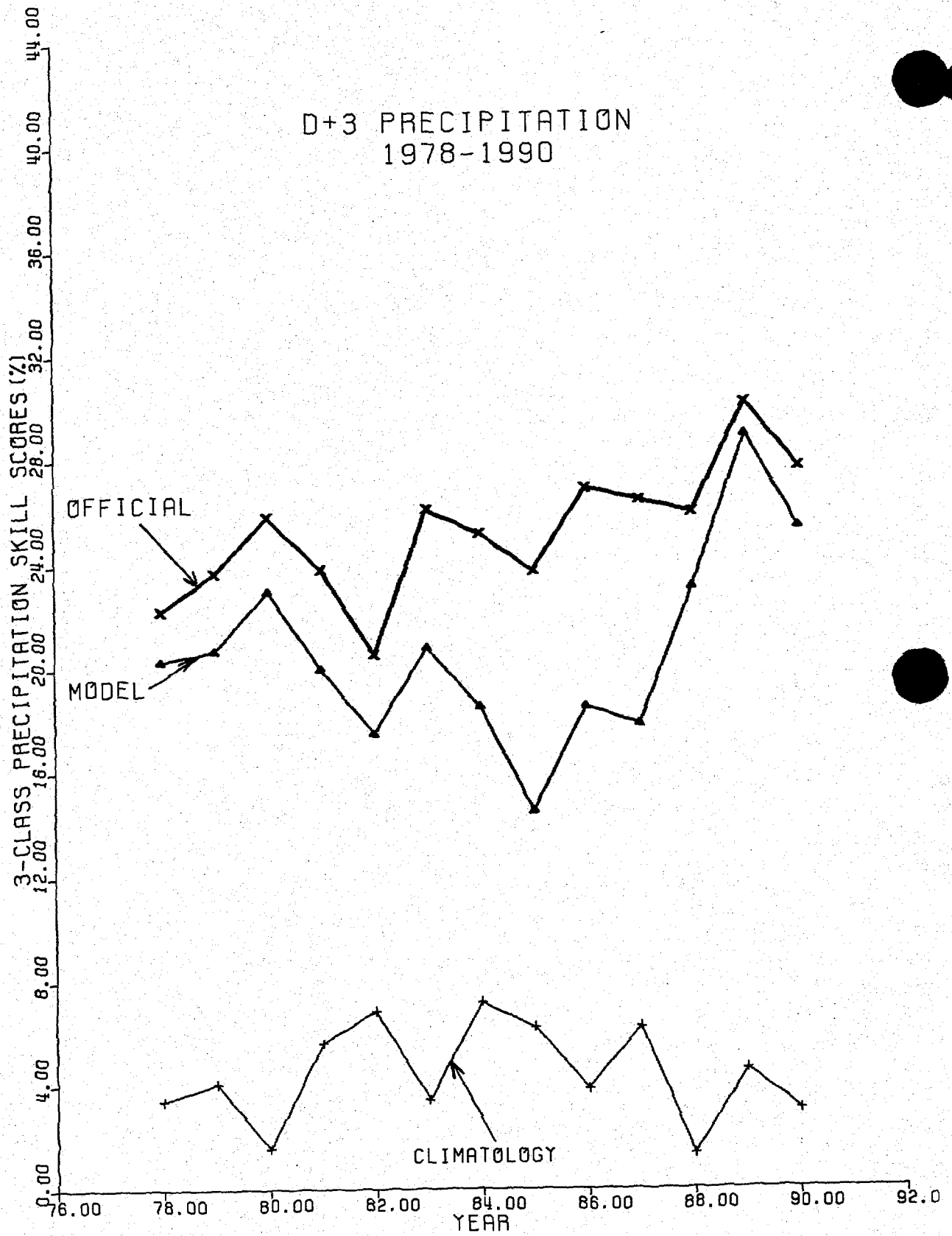


Figure 22

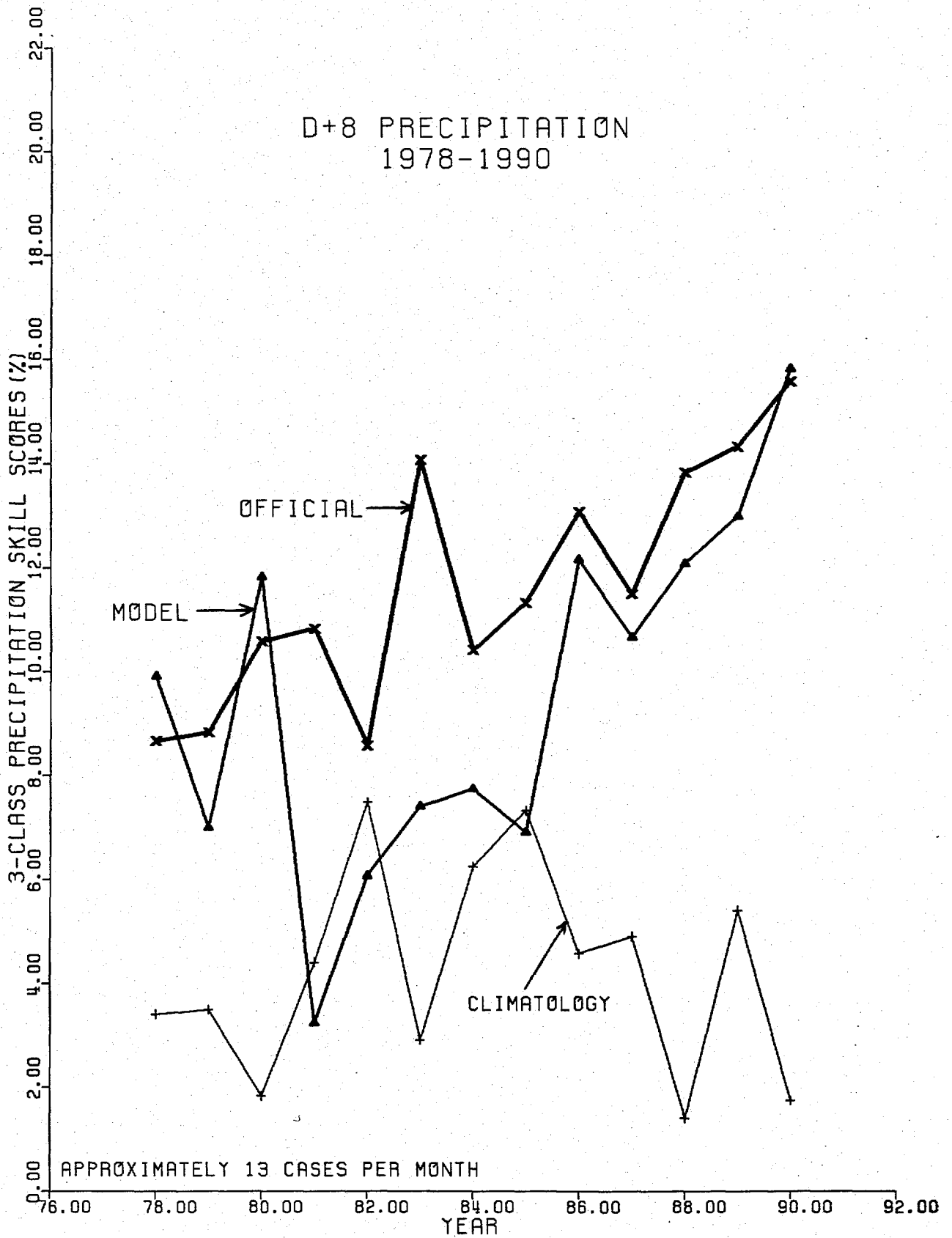


Figure 23

Appendix A

The standardized mean sea level pressure correlation score is used to determine the skill of the man and machine days 3, 4 and 5 mean sea level pressure forecasts. The correlation score is employed because the phasing instead of the intensity of systems primarily determines how well the various weather parameters can be forecast. The standardizing procedure prevents the contribution of the high variability (higher latitude) grid points from overwhelming the low variability grid points (lower latitude).

f = forecast mean sea level pressure at a grid point

o = observed mean sea level pressure at a grid point

σ = standard deviation at a grid point

n = normal mean sea level pressure at a grid point

$$F = \frac{f-n}{\sigma} \qquad O = \frac{o-n}{\sigma}$$

\bar{F} = average standardized forecast across n grid points

\bar{O} = average standardized observed across n grid points

$$\text{RMS } F = \sqrt{\bar{F}^2} \qquad \text{RMS } O = \sqrt{\bar{O}^2}$$

$$\text{RMS Error} = \sqrt{(\bar{F}-\bar{O})^2}$$

$$\text{Average Absolute Error} = |\bar{F}-\bar{O}|$$

$$\text{Correlation} = \frac{\bar{FO} - \bar{F} \bar{O}}{\sqrt{(\bar{F}^2 - \bar{F}^2)(\bar{O}^2 - \bar{O}^2)}} \times 100$$

Since the normal mean sea level pressure is subtracted from the forecast/observed pressure at each grid point, it is assumed that the correlation of the normal to the observed is always zero. Therefore, any positive score is considered

APPENDIX A (cont'd)

to have skill over the normal. Some doubts have been raised about this assumption, however, and for the past 5 years the unstandardized correlation score also has been calculated. This procedure allows a correlation score to be computed for the normal. This score then is simply the correlation of the forecast to the observed mean sea-level pressure.

APPENDIX B

The 5 day mean temperature skill score is a generalization of the Heidke skill score where the expected values are derived from the observed temperature

$$\text{Heidke Skill} = \frac{C-E}{N-E}$$

C = total correct (hits)

N = total number of forecasts (61)

E = expected number of hits

The expected value is calculated as follows from the number of stations in each of the observed temperature categories:

$$E = \frac{1}{8} \times \text{Much Below} + \frac{1}{8} \times \text{Much Above} + \frac{1}{4} \times \text{Below} + \frac{1}{4} \times \text{Above} + \frac{1}{4} \times \text{Normal}$$

The 5-day mean 3-class temperature skill score simply "lumps" together the much below with the below and the much above with the above. The expected (E) then is equal to $\frac{1}{4} \times \text{Below} + \frac{1}{4} \times \text{Normal} + \frac{1}{4} \times \text{Above}$.

Appendix C

The Gilman skill score is a generalization of the Heidke skill score where the expected values are derived from a randomized version of the precipitation forecast.

$$\text{Heidke Skill} = \frac{C-E}{N-E}$$

C = total correct (hits)

N = total number of forecasts (100)

E = expected number of hits

However, for a randomized forecast allowance must be made for stations having far different precipitation climate (N POP) across the United States. Therefore, to compute and score an expected chance forecast, climatology must be considered.

The procedure for this is as follows:

First, the actual number of forecasts of precipitation are distributed randomly taking into account station climatology. The expected number of chance hits is then given by:

$$E = \sum_{i=1}^N (p_i r_i + (1 - p_i)(1 - r_i)) \text{ or}$$

$$E = 2 \sum_{i=1}^N p_i r_i + N - \sum_{i=1}^N p_i - \sum_{i=1}^N r_i \quad (a)$$

where $r_i = 1$ for precipitation (≥ 0.01 inch) and 0 for no precipitation (< 0.01 inch).

Now an expression for p_i , which is the probability that after the forecast precipitation events are redistributed randomly a forecast precipitation event will fall at point "i" is given approximately by $p_i \approx \frac{F r_i}{\sum_{i=1}^N a_i} \quad (b)$. Here F = total number of forecasted precipitation events and a_i = climatic precipitation probability (N POP). This approximate value for p_i is most valid for small values of F and $(a_i / \sum_{i=1}^N a_i)$ and is unstable at times. Because of this instability the less sophisticated but more stable Hughes skill score was developed.

Substituting the expression (b) into (a) gives $E = \frac{2F \sum_{i=1}^N a_i r_i}{\sum_{i=1}^N a_i} + N - F - R$, where E = the approximate expected value of a randomized forecast, R = total precipitation cases, and N = total number of stations. If the climatic probabilities are uniform ($a_i = a_j = a$), then the approximate value of E reduces to the standard Heidke value given by: $E = \frac{(N-F)(N-R) + FR}{N}$.

APPENDIX D *

The 5-Day mean precipitation skill score is a generalization of the Heidke skill score where the expected values are derived from the observed precipitation:

$$\text{Heidke Skill} = \frac{C-E}{N-E}$$

C = total correct (hits)
N = total number of forecasts (100)
E = expected number of hits

For example, in January the number of stations in the area covered by the (NP/P), (NP/M/H) and (L/M/H) categories is 21, 28 and 51 respectively. The average value of the probability of NP for the stations in the (NP/P) area is 70% and 40% in the (NP/M/H) area. Now if (NP/L) is coded as 1, M as 2 and (P/H) as 3, then the number of stations expected to have coded value 1 thru 3 is as follows:

33% of (L/M/H) = $51 \times .33 = 17$ stations coded 1, 2, 3

40% of (NP/M/H) = $28 \times .40 = 11$ stations coded as 1 and 8.5 coded as 2,3

70% of (NP/P) = $21 \times .70 = 14.7$ stations coded as 1 and 6.3 coded as 3

Thus, code 1 = $17 + 11 + 14.7 = 42.7$ stations
code 2 = $17 + 8.5 = 25.5$ stations
code 3 = $17 + 8.5 + 6.3 = 31.8$ stations
100.0 stations

Therefore, the expected value = $.427a + .255b + .318c$

where a, b and c are the number of coded values 1, 2 and 3 observed.

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FEB 25 1991

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